



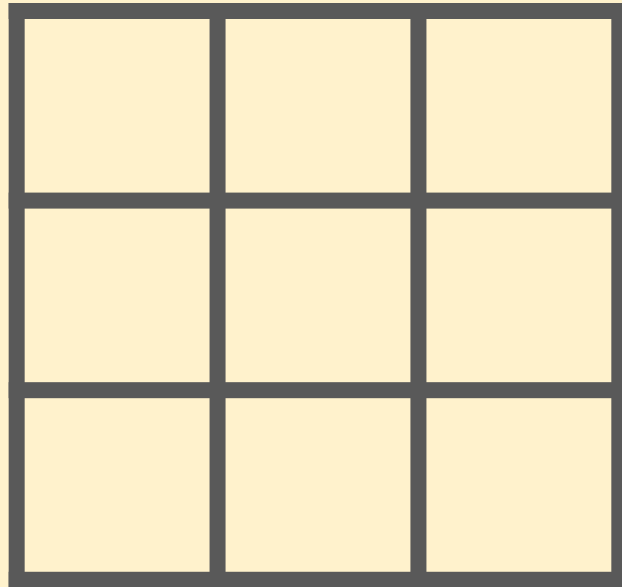
The Global Math Circle

# Using Magic Squares in Math Circles of all ages, ability levels and topics

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Joint Mathematics Meeting 2023

Using the numbers 1 through 9, create a square whose rows, columns, and diagonals all sum to the same number.





# The Global Math Circle



*Discovering  
math  
together*



# Re-imagining Math Education for 21st century learners



	1	
		
		

A	B	C
D	E	F
G	H	I

$$A + E + I = 3N$$

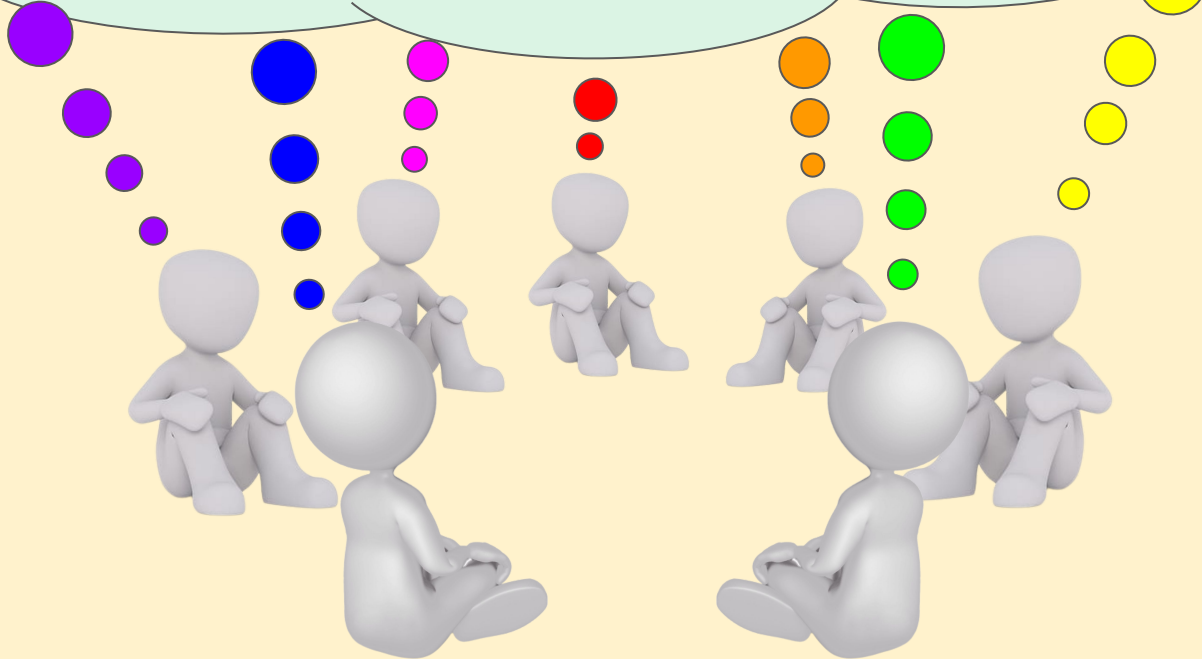
$$C + E + G = 3N$$

$$B + E + H = 3N$$

$$3E = N$$

M	N	?
?	$K=3N$	?
?	H	I

$$C = 3K - (M+N)$$

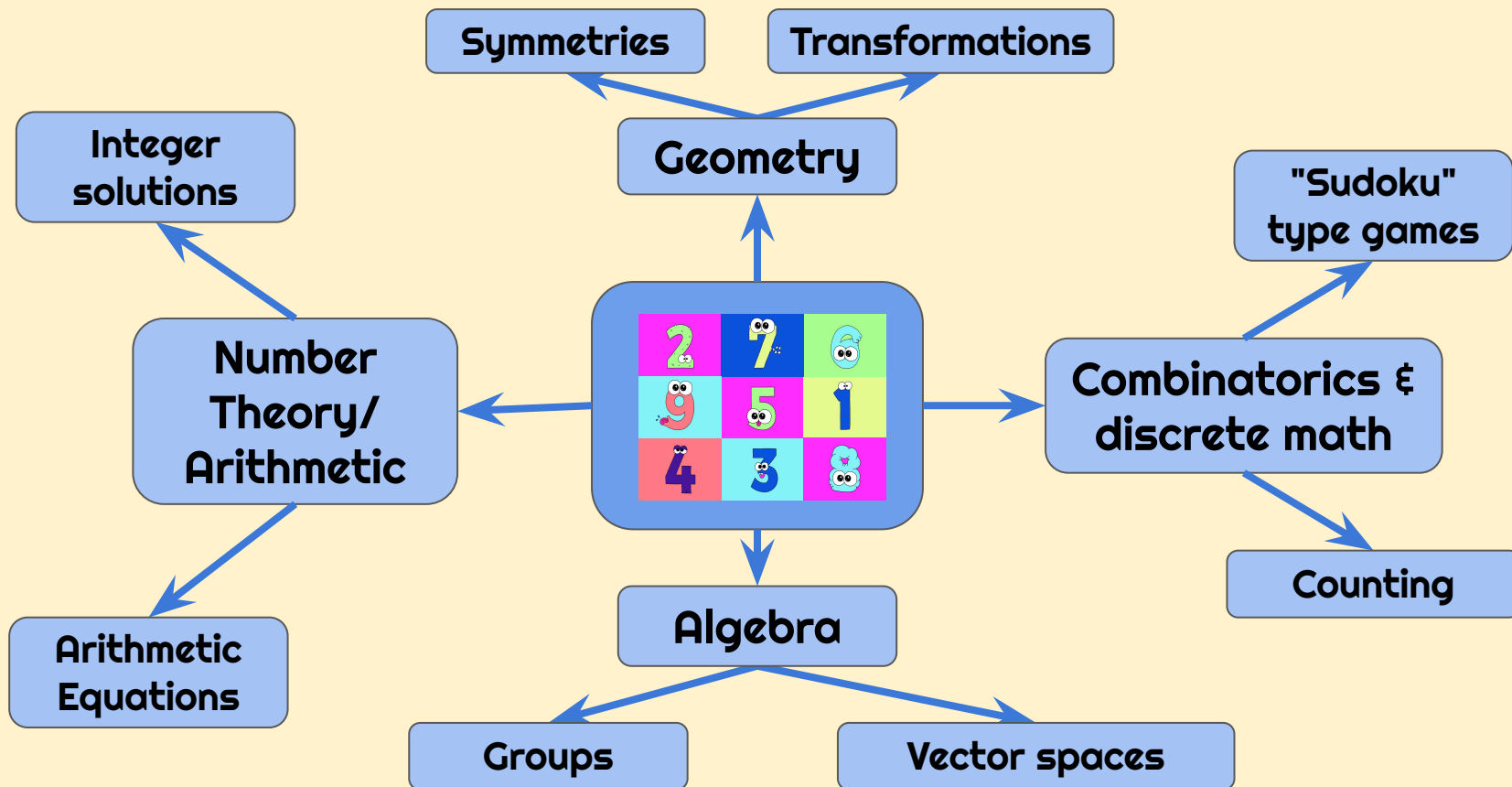


Using the numbers 1 through 9, create a square whose rows, columns, and diagonals all sum to the same number.

*This is our  
accessible  
mystery*

	7	6
		1
4	3	8

# Magic squares can take us in many directions



We have successfully run this circle five times with different groups

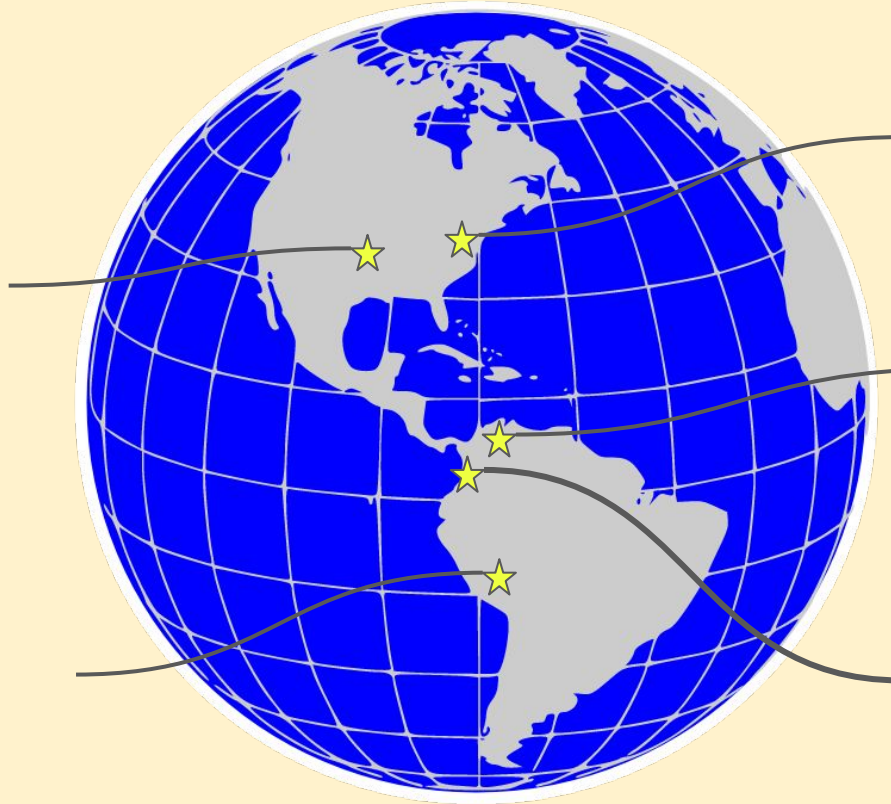
**2022:** American & Canadian online students 11-13 years old

**2020:** American online students 8-10 years old

**2022:** Indigenous Colombian students

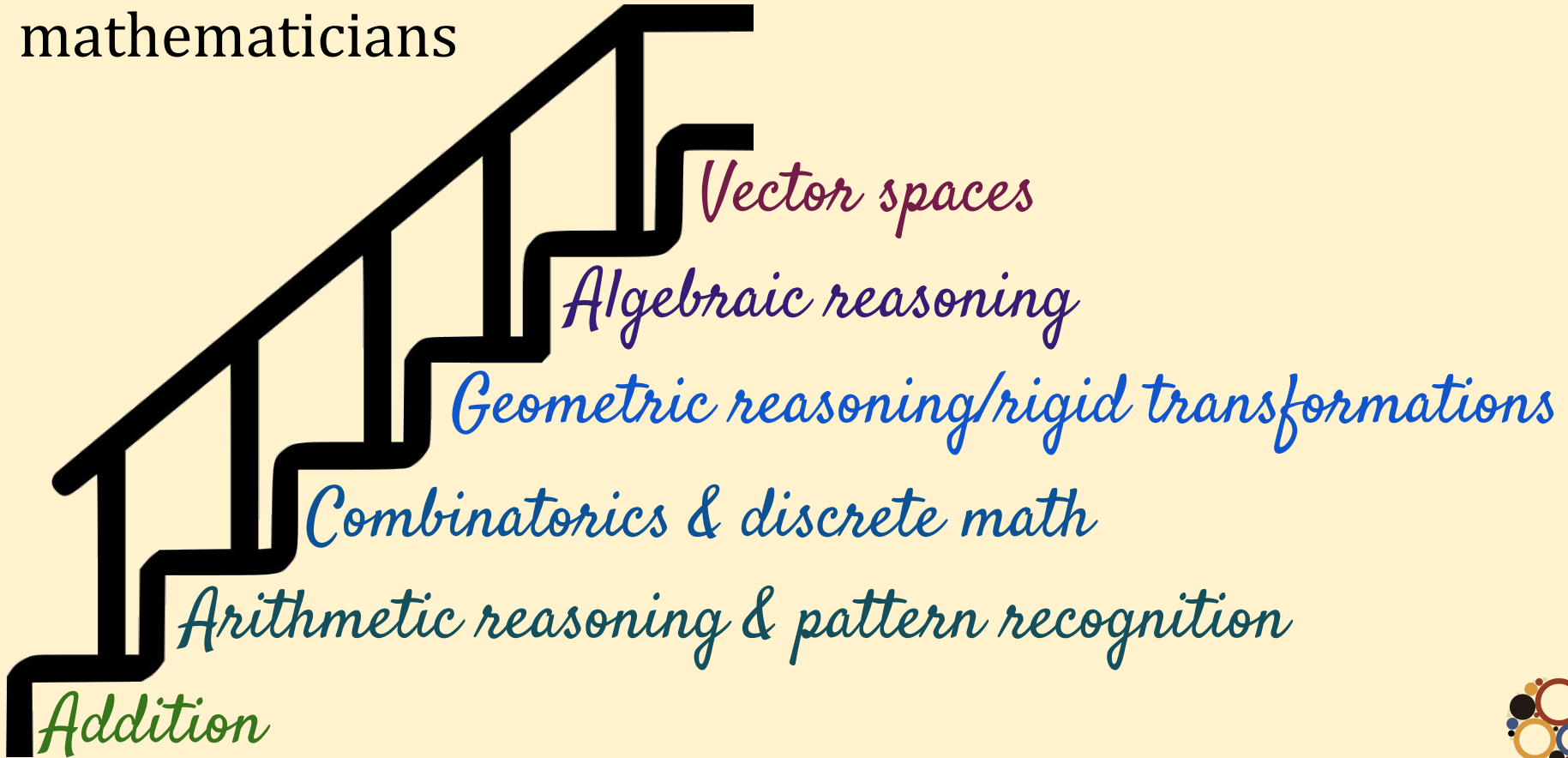
**2021:** Peruvian 13-15 year old students

**2021:** Colombian students online





Magic squares are accessible by all levels of young mathematicians



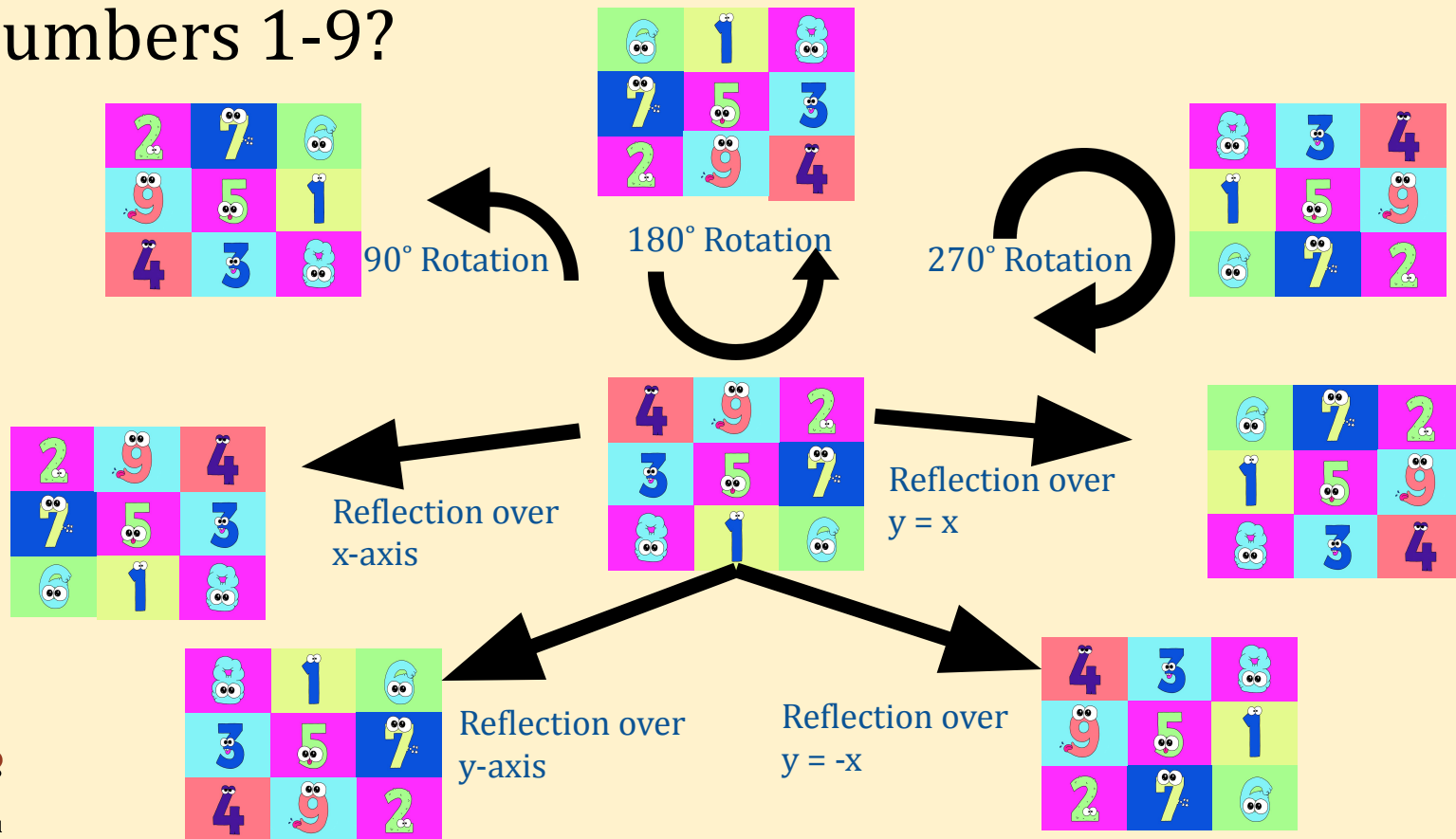
# Arithmetic reasoning & pattern recognition

*What is the sum of each row, column, and diagonal?*

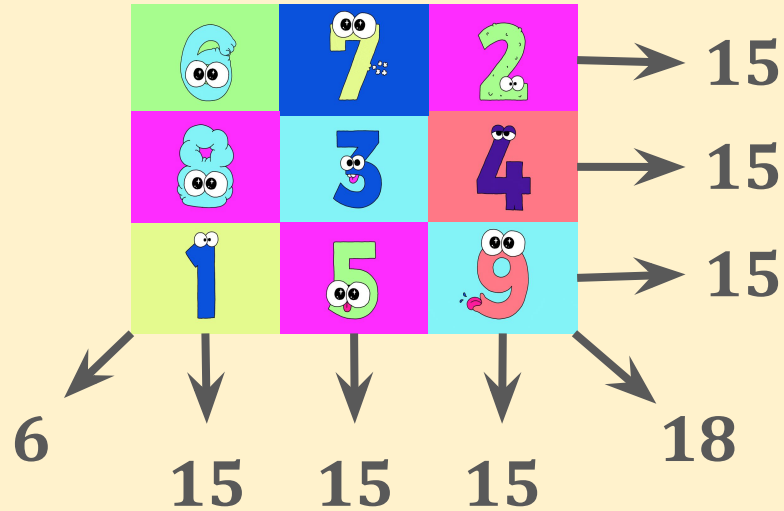
*Which sum appears the most? Why do you suppose that's the case?*

1	2	3
4	5	6
7	8	9

# How many 3x3 magic squares are there using the numbers 1-9?



# Semi-magic Squares and Tiling (Translations)



# Semi-magic Squares and Tiling (Translations)



# Using structure to help you find relationships

A	B	C
D	E	F
G	H	I

Can you prove that the sum of all rows columns and diagonals in a magic square would equal  $3E$ ?

Given three numbers, can you complete the magic square?

3	1	
	2	



Given three variables, can you complete the magic square?

$n$	$m$	
	$k$	





# Magic squares are preserved under addition

The image illustrates the addition of two 3x3 grids of numbers, each with a cartoon face, to produce a third 3x3 grid. The numbers in the first grid are 6, 7, 2; 8, 3, 4; 1, 5, 9. The second grid has 1, 2, 8; 8, 1, 2; 2, 8, 1. The resulting grid has 7, 9, 2; 8, 4, 6; 3, 5, 10.

6	7	2
8	3	4
1	5	9

+

1	2	8
8	1	2
2	8	1

=

7	9	2
8	4	6
3	5	10

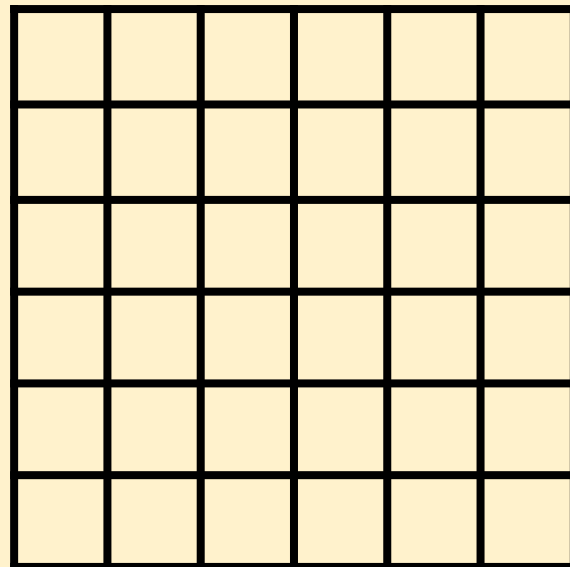
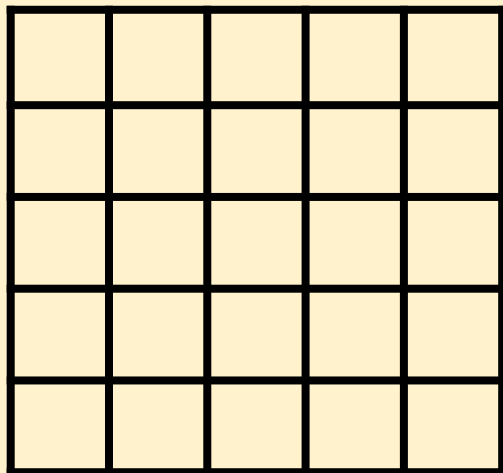
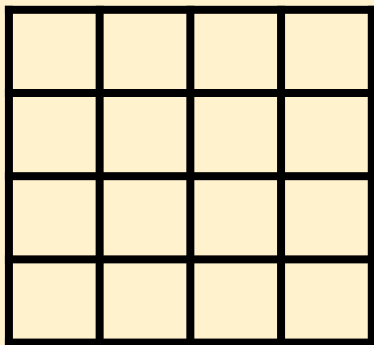
# Magic squares are scalable

4	9	2
3	5	7
8	1	6

$$\times 3 =$$

12	27	6
9	15	21
24	3	18

# Giant magic squares



# Giant magic squares

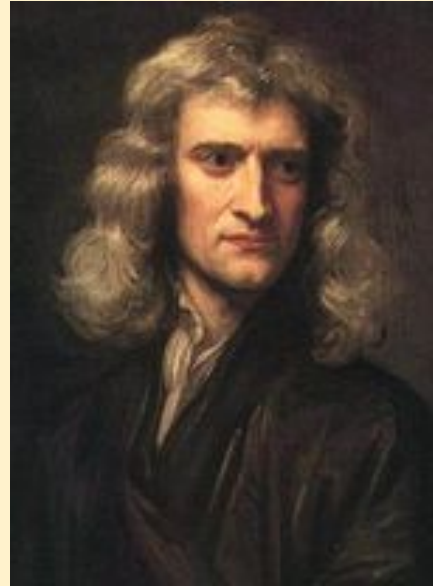
*Using the base of the 3x3 magic square, can you complete this 5x5?*

5	5	5	5	5
5	4	9	2	5
5	3	5	7	5
5	8	1	6	5
5	5	5	5	5



"If others would think as hard as I did, they would get similar results."

-Isaac Newton



Thank you!



<https://www.theglobalmathcircle.org/>